



## Time Effects on Cu-Zn-Al Shape Memory Alloys

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Reliability is a critical word in industrial applications of Shape Memory Alloys (SMA) usually called smart materials. Applications of these materials require a rigorous stability of the transformation temperatures and a small hysteresis. The applications of the SMA to the continuous actuators involve a time guarantee about the constructed devices related to the suitable composition and heat treatment. From a mechanical model for a single martensite plate, the shape of the hysteresis cycle (single crystal of Cu-Zn-Al alloys) is obtained by generalizing the representation to  $N$  plates. The observed time effects on the hysteresis loops related to diffusion processes were also taken into account. They allow to explain the martensite recoverable creep and the micromemory effects. Using high resolution on resistance measurements, the room temperature effects on the parent phase acting over the transformation temperature  $M_s$  is evaluated. The effect produced by two atomic order parameters (*i.e.* B2 and L2<sub>1</sub>) related to the yearly room temperature evolution (for instance, summer to winter) induces predictive evolution of transformation temperature and the mean uncertainty reduces drastically ( $\delta M_s \approx \pm 0.05$ ).

### 1. Introduction

Smart materials carry out simultaneous functions as sensors and actuators. One of them, the memory alloys are distinguished by a martensitic transformation between metastable phases [see, 1-9 as general references]. The high temperature crystallographic form (or austenite) is coherent with a large number of variants in the low temperature structure (or martensite). This allows for various macroscopic shapes in the low temperature phase to coexist with only one high temperature shape (Shape Memory Effect). Only in a highly particular situation the reverse process produces new orientation.<sup>10</sup>

The main interest on continuous actuators focuses only in the coexistence domain (from 0 to 100 per cent of martensite phase) and in small hysteresis as copper based alloys. The industrial interest needs an experimental method classifying the ability of available alloys. Recent

improvements relate with the availability of appropriate stored data or representative models.<sup>11-15</sup> Likewise, physical image models have been built for single crystals, starting from the detailed behaviour of single variant martensite domains or plates.<sup>16-19</sup> Recently, numerical routines have been established for the construction of devices in SMA<sup>20-21</sup> and some models have been described which include the perturbations introduced by the heat transport towards the surroundings.<sup>22-23</sup>

The applicability of the material for on-off actions need only a poor reliability. Usually, the phase changes are produced by an electrical current pulse and its associated change of temperature is fairly high. To avoid spontaneous changes of the material, it is convenient to use alloys which have a considerable hysteresis. Within this group of applications, TiNi microactuators can be found (see [24] and related references). Recently, techniques for the production of thin films on TiNi have

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been developed by Ar-plasma deposition directly in crystalline form (without ageing at high temperature).<sup>25</sup> In a continuous and smooth control, we need a small hysteresis and the rigorous stability of the transformation temperatures: a time guarantee is required for constructed devices. The transformation temperature depends on thermal treatments or, in equivalent form, on the degree of atomic order in the material (see, for instance [7, 26-28] and related references). Recently, it has been detected an increasing interest in the degree of atomic order and its evolution with time.<sup>29-33</sup> A careful analysis (accuracy  $\pm 1$  K) of the evolution of the transformation temperature needed to establish the limits of guarantee of the Thermomark can be found in reference 34. This device is used to guarantee the safekeeping of frozen products. The analysis of the experimental results indicates that the transformation temperatures fluctuate "pseudo-randomly" in long term observations within relatively reduced margins ( $\Delta M_s \approx \pm 2$  K). In general, the changes in  $M_s$  have been associated to many causes: atomic order (B2 and L2<sub>1</sub> in Cu-Zn-Al alloys), domains of order, elastic dipoles, dislocations (creation, movement and evolution), ...

In this work, we describe the behaviour of the material with the help of a physical image model (single crystal with one or more single variant). The experimental observations allow the inclusion of the local modifications in the equilibrium temperature produced by the coexistence of the two phases. This permits to explain the phenomena of martensite creep,  $\beta$  recovery, .... By carrying out continuous observations of the electrical resistance in austenite phase and using a rigorous control and programming of the temperature, it is possible to quantify the behaviour of the material near room temperature. The analysis of the experimental results allows phenomenological rules which regulate the behaviour of the material as functions of time and room temperature. The results establish that the uncontrolled fluctuations of the transformation temperature can be strongly reduced ( $\delta M_s \approx \pm 0.05$  K).

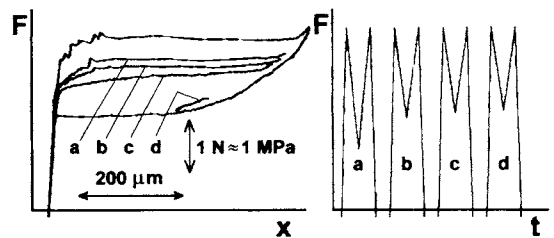
**2. Coexistence processes:  
stress-strain-temperature-time**

A series of global and partial stress-strain cycles have been carried out using high resolution adapted equipment described elsewhere.<sup>35-38</sup> Cu-Zn-Al single

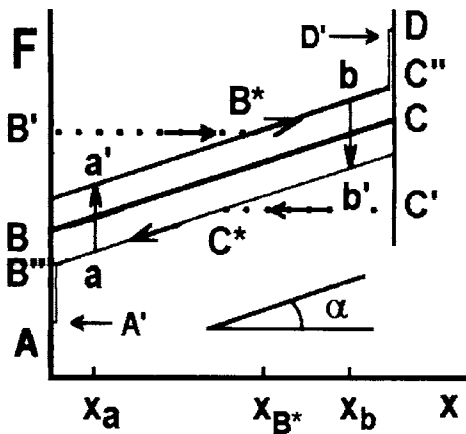
crystals (electronic concentration 1.48 e/a) were used.

The samples were cut with the appropriate crystallographic orientation to obtain the maximum deformation (around 9 per cent) in b.c.c. to monoclinic ( $\beta \rightarrow \beta'$ ). The available transformation length  $l$  of used samples is around 4 mm, near 1 mm<sup>2</sup> of the cross section and standard  $M_s$  near 280 K. The observations have allowed the visualization of the effects of the nucleation in the martensite phase, the effect of the intrinsic thermoelasticity produced by the interaction of the interphase with the pre-existing dislocations, the friction related to the interphase movements, the coalescence of the martensite limits in the same variant and related phenomena.

A thermomechanical model is described, like the one in page 305 of ref. 39, coherent with the experimental observations of a single martensite plate. The sample is divided in  $N$  domains (or plates) of transformation-retransformation. The maximal deformation is 9 per cent ( $X_{max} = 0.09 \ell$ ) and the related lengthening for each plate ( $x_{max}^0$ ) is  $0.09 \ell / N$ . Increasing the stress or the external force  $F_{ext}$  the lengthening  $x$  of each plate increases from zero to  $x_{max}^0$ . In general, the actual lengthening  $x$  is a function of external force, temperature  $T$  and previous path or history. The Fig. 1 visualizes the relevant unloading needed to recover completely the parent phase without thin martensite microplates. In Fig. 2, the path of the working point is presented for only one domain avoiding contributions related to classical thermal expansion and elasticity. Trajectory corresponds to the coordinates  $F-x$ , to the transformation from the austenitic phase to the martensitic phase and back-ward.<sup>17-19</sup> For instance, in loading, the path



**Fig.1** Experimental hysteresis behavior in single crystal, single variant transformation with several martensite plates. The hysteresis width increases with the achieved unload in internal loop.



**Fig. 2** Model for each martensite plate: trajectory in  $F$  (force or stress) against lengthening  $x$ .

presented in **Fig.2** corresponding to the  $i$ -th plate becomes:

in path  $AB'$ ,

$$F_{ext} < f_{00}^{(i)} + z_{n0} + z_{if} \quad \text{with } x^{(i)} = 0$$

at  $B'$  and  $B^*$  points,

$$F_{ext}^{B'} = F_{ext}^{B^*} = f_{00}^{(i)} + z_{if} + \left[ \frac{df}{dx} \right] x_{B^*} \quad \text{and } x^{(i)} = x_{B^*}$$

at  $D$  point,

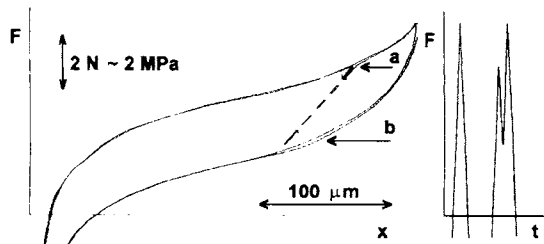
$$F_{ext}^D = f_{00}^{(i)} + z_{if} + \left[ \frac{df}{dx} \right] x_{max}^0 \quad \text{and } x^{(i)} = x_{max}^0$$

in path  $DC'$ ,

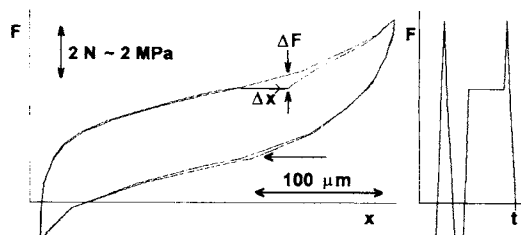
$$F_{ext} > f_{00}^{(i)} - z_{n1} - z_{if} + \left[ \frac{df}{dx} \right] x_{max}^0 \quad \text{and } x^{(i)} = x_{max}^0$$

On cycling symmetric behavior is used. From austenite to martensite, the path on loading describes  $A, B, B'$  (nucleation),  $B^*$  (after nucleation),  $C''$  (only traces of parent phase),  $D'$  (complete coalescence with the nearby plate), ...; from martensite to austenite the path describes  $D, C, C'$  (b nucleation),  $C^*$ ,  $B''$  (unrelevant length),  $A'$  (complete disappearance). Path  $a, a', b, b'$  is an internal loop with friction related to the movement of interfaces without nucleation; the slope  $\alpha$  is a macroscopic effect of the internal thermoelasticity: an interaction between interface and preexistent dislocations. Using a series of  $N$  domains, the global and partial (internal loops) hysteresis cycles *without time effects* are simulated accurately.<sup>18</sup>

When disturbances on the trajectory of the

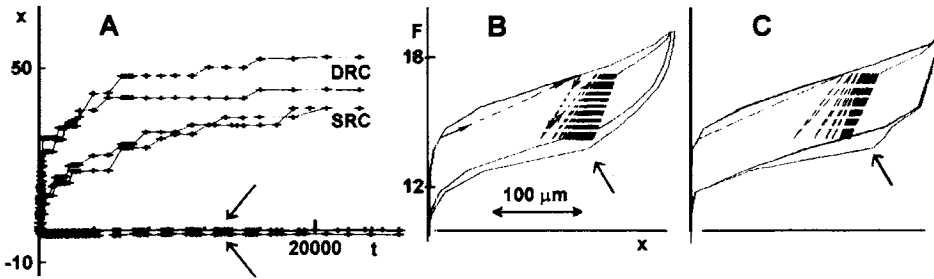


**Fig.3** Left: hysteresis cycle on force  $F$  against lengthening  $x$  at constant temperature; effect of a force fluctuation (only the extreme points are presented); a) martensite creep; b) "micromemory" effect. Right: force against time (schematic).



**Fig.4** Left: hysteresis cycle on force  $F$  against lengthening  $x$  at constant temperature;  $\Delta x$  increase of transformed material at constant load;  $\Delta F$  related change of load: the arrow indicates the micromemory effect. Right: force against time (schematic).

hysteresis cycle are carried out, it can be observed an increase in the amount of martensite (**Fig. 3**) and a minor micromemory effect. The process could be associated with the reordering of domains by the differences between the frictions from the various martensite plates. This interpretation is insufficient. In fact, martensite creep at constant stress (**Fig. 4**) can be observed. The evolution of the amount of martensite at constant stress (**Fig. 5(A)**) reaches a steady value after approximately 10 hours. The increase can be associated to the coexistence of the two phases and, eventually, to the previous movement of the interphases. The SRC evolution (static recoverable creep) is obtained loading at very low stress rates: the analyzed point is reached at  $ds/dt < 1 \text{ kPa s}^{-1}$ . When the approximation occurs at a greater stress rate ( $< 10 \text{ kPa s}^{-1}$ ) an increased creep (DRC or dynamic recoverable creep) is observed. The effects associated with the latent heat are observed for higher stress rates (near  $50 \text{ kPa s}^{-1}$ ). From the series of



**Fig. 5** A) lengthening against time; the arrows indicate the creep effect on unloading; B) experimental: hysteretic behavior with internal loops (only the end points are represented), the arrow indicates the micromemory effect; C) associated simulation. Working temperature used: 290.7 K.

experimental observations, it is derived that the equilibrium temperature  $T_0$  of one or more domains of the sample is affected by the coexistence of the two phases. The SRC and DRC effects are calculated from the value of  $\Delta F/\Delta x$ , which is determined from Fig. 4 and the value of  $(dF/dT)_{CC}$  (Clausius-Clapeyron equation)\*1. The experimental value of  $(dF/dT)_{CC}$  is derived from the values of  $F$  on homologous points of the hysteresis cycles carried out at different temperatures. The creep effect is a function of the position in the hysteresis cycle. It is lower in the initial part of loading (minor number of active plates) and at the end part (practically no parent phase available). On unloading, reversal of the frictional actions "freezes" the creep effect (see the arrows in Fig. 5(A)). During long term observations, several days at constant stress, it is possible to detect a further smaller increase on  $T_0$  probably related with the LTT time evolution on parent phase (see below).

The local evolution of the equilibrium temperature for each plate  $\Delta T_0(t)$ , can be expressed as [19]:

$$\Delta T_0(t) = \Delta T_0^{SRC}(1 - e^{-t/\tau^{SRC}}) + \Delta T_0^{DRC}(1 - e^{-t/\tau^{DRC}})$$

$$\Delta T_0^{SRC} = 0.5 \text{ K} ; \Delta T_0^{DRC} = 0.2 \text{ K}$$

$$\tau^{SRC} = 6000 \text{ s} ; \tau^{DRC} = 200 \text{ s}$$

If the external stress is reduced, the material goes again to  $\beta$  phase, which progressively recovers the initial value of the equilibrium temperature  $T_0$  ( $\beta$  recovery). The observations suggest that the approximation to the

reference state follows an exponential form, from the initial value after the previous coexistence process:

$$\Delta T_0^\beta(t) = \Delta T_0 e^{-t/\tau^\beta} ; \tau_\beta \approx 300 \text{ s}$$

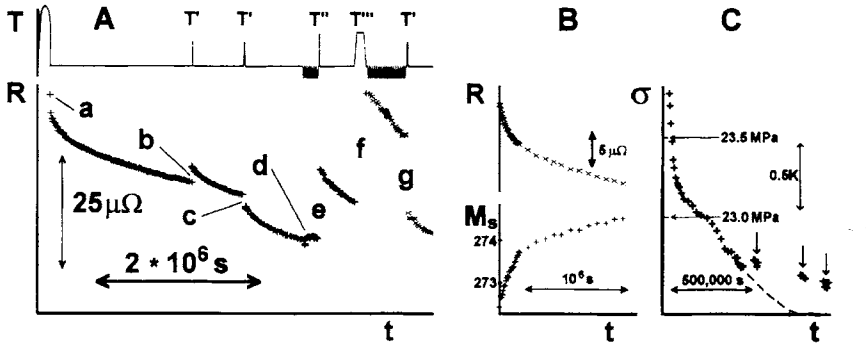
In Fig. 5(B) experimental stress-strain or force-displacement cycles with internal loops are shown. Only the extreme points have been presented in partial cycles. Fig. 5(C) is the corresponding computer simulation. The arrows indicate the appearance of the micromemory effect in unloading.

### 3. Time evolution on parent phase

Computer controlled electrical resistance measurement system which allows a resolution and reproducibility of around 0.05 % (stress free) has been used. Continuous observations have been carried out during more than 3 years with the temperature controlled. Starting from several temperatures  $T$  in a steady state, cooling to martensite (263 K) and subsequent heating produces a complete cycle of the transformation-retransformation and the  $M_s$  value can be determined from the experimental cycle  $R = R(T)$ . The sample used (Cu-Zn-Al) has an electronic concentration 1.48 e/a, and the nominal  $M_s$  arounds 270 K.

In Fig. 6(A), the evolution of the electrical resistance at 293 K (in parent phase) can be observed after soldering the wires on the sample. A general decrease is noted, which fluctuates according to the type of immediate action carried out; microflash heating in the b point (temperature 348 K), 10 hours in the c point, cycling process in d, heating at 363 K by 1 hour in e point, ageing at 365 K by 12 hours in f point and similar to c in g point. The decrease of the resistance is

\*1) Fatigue test using INSTRON's equipment and higher stress rates (cycling at 0.8 Hz) produces similar but increased effects as greater as 10 K.<sup>40)</sup>

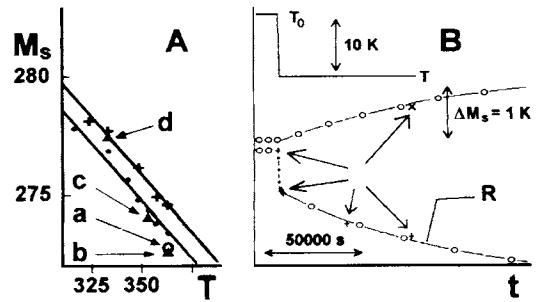


**Fig. 6** A-top) temperature against time (schematic); A-bottom) resistance versus time with the action of several micro heat treatments; B) resistance R and transformation temperature M<sub>S</sub> against time using two cycling frequencies; C) critical stress vs. time, - - - expected evolution; arrows indicates the actual values after several days without cycling.

associated to an increase in the transformation temperature and the process speeds up when cycling. In **Fig. 6(B)**, it can be observed the evolution of the resistance and that of M<sub>S</sub> for two cycling rates after a microheating. The evolution process of the equilibrium temperature is similar if the system is maintained at a constant temperature and the transformation-retransformation cycles are stress induced (**Fig. 6(C)**).

Together with a decreasing evolution of the resistance, **Fig. 6(A)** presents "stochastic" characteristics. See, for instance, the resistance evolution in b and c points associated to the same ageing temperature. With the aim of quantifying the evolution processes and eventually the "uncertain" effects, measurements at various constant temperatures have been carried out. From the series of observations, the existence of a relation between the time constant for the nearly-exponential evolution of resistance and the temperature has been observed, with an activation energy of 1.17 eV. The evolution of the transformation temperature after a temperature step (several hours or days) at room temperature implies an evolution in the state of order of the material and it could be considered that it is linked to the evolution of the B2 order, corresponding to the nearest neighbours atoms .

Once the steady state has been reached, the value of M<sub>S</sub> is approximately linear with the ageing temperature T on parent phase (see the + + + on **Fig. 7(A)**). The slope value (dM<sub>S</sub>/dT) approaches -0.105. The action of a temperature step near room temperature (from T<sub>0</sub> to



**Fig. 7** A) M<sub>S</sub> against ageing temperature; + + + first series of measurements; ● ● ● second series of measurements; a) after several partial times on 363 K, b) steady state on 363 K; c and d) other steady states; B) M<sub>S</sub> and resistance behavior after a temperature step (from T<sub>0</sub> to T); - - - calculated values; (x or +) experimental values.

T) produces changes on transformation temperature: M<sub>S</sub> displays nearly an exponential behaviour (see, **Fig. 7(B)**). Starting in a steady state at T<sub>0</sub>, the M<sub>S</sub> after a room temperature step (from T<sub>0</sub> to T) at time t<sub>ref</sub> reads,

$$M_S(T, t) = M_S(T_0) + \Delta M_S^{B2} (1 - e^{-(t-t_{ref})/\tau^{B2}}) ;$$

$$\Delta M_S^{B2} = -0.105(T - T_0)$$

with

$$\tau^{B2/s} = \exp(-29.304 + \frac{13630 \text{ K}}{T})$$

The previous relations allow a predictive

**Table 1** Relative time evolution of near-neighbours order: experimental and calculated effect on Ms (in K) after H hours ( $H \equiv t - t_{ref}$ ) of a temperature step (from  $T^0$  to  $T$ ); experimental, predicted and difference  $\delta M_s$ ; the  $T^0$  value is 358.15 K.

H/h	T/K	$M_s$ /K(exp)	$M_s$ /K(calc)	$\delta M_s$ /K
4.0	333.15	275.47	275.22	0.25
12.0	333.15	275.81	275.80	0.01
24.0	333.15	276.29	276.43	-0.13
59.4	305.65	275.28	275.23	0.05
59.4	293.15	274.83	274.93	-0.10

approximation to the values of the transformation temperature (see Fig. 7 (B) and Table 1). The average difference ( $\delta M_s$ ) between the calculated temperature and the experimental is less than 0.1 K in experiments lasting a few days.

The detailed observation of the resistance evolution for extended periods of time visualizes the LTT or Long Time Tail effects: a slight decrease in its value (41). Also, the relation between  $M_s$  and the ageing temperature is modified if the sample remains at "higher" temperatures (363 K) during a long period of time. After several hundreds of macro-cycles made up of an ageing of 9 hours at 363 K followed by ten cycles of transformation-retransformation the  $M_s$  changes to the point a in Fig. 7 (A). Once the sample has spent 1008 ks (accumulated in five months) at a temperature of 363 K and, after 13 days at 333 K, the behaviour of  $M_s$  with regards to the ageing temperature is equivalent but decreased (see the points ●●●● in Fig. 7 (A)).

The long term analysis (LTT) allows for quantitative estimates of the residual evolution of the resistance which can be associated to L2<sub>1</sub> order. From the experimental curves, a second time constant with an activation energy of 0.79 eV can be estimated. Departing from the experimental observations in LTT steady state (points b, c and d in Fig. 7 (A)) an amplitude of  $M_s$  fluctuation is evaluated. Once the sample *effectively* finds a steady state at temperature  $T^0$ , the  $M_s$  after a temperature step (from  $T^0$  to  $T$ ) at time  $t_{ref}$  reads:

**Table 2** Time-temperature effects on  $M_s$ ;  $T^0$  steady state temperature;  $T$ : actual temperature;  $H$ : elapsed time in days ( $H \equiv t - t_{ref}$ ); b, c, d indicated on figure 7(A), (\*) reproducibility of independent measurements; (†): asymptotic values (steady state conditions);  $\delta M_s$ : difference between experimental and calculated values.

$T^0$ /K	T/K	H/day	$M_s$ /K(exp.)	$M_s$ /K(calc.)	$\delta M_s$ /K
	363.2	7(†)	272.52	b(*)	
	353.2	15(†)	274.02	c	
	333.2	26(†)	277.44	d	
	363.2	8(†)	272.32	(*)	
363.2	343.2	4.59	275.30	275.33	-0.02
345.7	325.5	10.1	277.30	A	277.52 -0.22
345.7	295.2	30.4	278.75	B	278.71 +0.04
345.7	295.2	55.8	279.06	C	279.05 +0.01

$$M_s(T, t) = M_s(T^0) + \Delta M_s^{B2} (1 - e^{-(t-t_{ref})/\tau^{B2}}) + \Delta M_s^{L21} (1 - e^{-(t-t_{ref})/\tau^{L21}})$$

with the same parameters for the "fast" B2 evolution, and, further:

$$\Delta M_s^{L21} = -0.067 (T - T^0)$$

$$\tau^{L21}(s) = \exp(-16.933 + \frac{10330 \text{ K}}{T})$$

The time constant values associated with process L2<sub>1</sub> are very high: from 100 °C to 25 °C, the  $\tau^{B2}$  changes from 1400 s to 155 days and the related  $\tau^{L21}$  changes from 0.54 days to 1.6 years. The seasonal actions or summer and winter effects are then smoothed by the time constants value.

From the expressions associated to a Heaviside step after an steady state, it is possible to deduce the effect on  $M_s$  of a disturbance of the temperature or a Dirac pulse  $\delta T^0$  produced in  $t=0$ . Starting on the previous steady state, the  $M_s(\delta T^0, t)$  reads:

$$M_s(\delta T^0, t) = M(T^0) - \frac{0.105}{\tau^{B2}} e^{-t/\tau^{B2}} - \frac{0.067}{\tau^{L21}} e^{-t/\tau^{L21}}$$

Starting from a steady state seems possible to calculate the value of  $M_s(t)$  produced by the evolutions of the room temperature with the use of a non-linear convolution. Preliminary reproducibility and reliability of the prediction for all effects are shown in Table 2. Starting at steady state at 345.7 K, the A, B and C values relate a long lasting "room temperature" evolution

with a cooling of 2 K day<sup>-1</sup> from 345.7 K to 295.2 K (final constant temperature). The quantification of the LTT effects allows for an increased reduction in the fluctuations on  $M_s$  in long lasting analysis. In general, the effects of the seasonal evolution of the temperature (summer-winter, *i.e.* greater than 20 K) affects the value of the  $M_s$  up to 17 % of the room temperature fluctuation (around 4 K) but the action is smoothed and delayed by the time constant values.

#### 4. Conclusions

The particular behaviour of the SMA is associated with a phase transition between metastable phases. This implies the possibility of evolutions in the material. Its applicability as a continuous actuator with a long term guarantee requires an exhaustive quantification of its properties and subsequently, to mark out the limits of variability. Using high resolution equipment allows the carrying out of quantitative observations and to modelize its behaviour.

Using single crystals and single variant transformations allow for the quantification of the physical parameters of the process (nucleation, coalescence, friction between the interfaces, intrinsic thermoelasticity and the time coexistence effects), and to build a physical image model which supplies completely coherent results with the experimental observations. In the case of Cu-Zn-Al (electronic concentration 1.48 e/a), a recoverable evolution at low stress rates ( $\leq 10$  kPa/s) is observed on the equilibrium temperature (around 0.7 K) when both phases coexist. This corresponds to the phenomena of martensite creep and micromemory.

To interpret the processes of ageing near room temperature only two ordering processes are required (for instance, B<sub>2</sub> and L<sub>21</sub> atomic orders). Starting from a steady state, it is possible to predict quantitatively the transformation temperature from the evolutions of the room temperature by means of a non-linear convolution. For the studied alloy, the yearly effects (summer-winter) of the room temperature fluctuations produce changes in the transformation temperature near 2 K. The applied working methodology to characterize the time dependence of SMA behavior has proved to be successful to reduce the stochastic components on transformation temperature  $M_s$  and to evaluate the particular parameters of the used alloy.

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